

A model for distortions of polarisation-angle curves in radio pulsars

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ABSTRACT

Context. Some radio pulsar profiles (in particular those of millisecond pulsars) contain wide emission structures which cover large intervals of pulse phase. Local distortions of an average curve of polarisation angle (PA) can be identified in such profiles, and they are often found to be associated with absorption features or narrow emission components.

Aims. The features may be interpreted as a convolution of a lateral profile of an emitter with a microscopic radiation pattern of a non-negligible angular extent.

Methods. We study a model which assumes that such an extended microbeam of the X-mode curvature radiation is spreading the radiation polarised at a fixed position angle within an interval of pulse phase.

Results. The model is capable of interpreting the strongly dissimilar polarisation of double notches in PSR B1821–24A (for which we present new polarisation data from the Nançay Radio Telescope) and PSR J0437–4715. It also explains a step-like change in PA observed at the bifurcated trailing component in the profile of J0437–4715. A generic form of the modelled PA distortion is a zigzag-shaped wiggle, which in the presence of the second polarisation mode (O mode) can be magnified or transformed into a W- or U-shaped deflection of a total net PA.

Conclusions. The model's efficiency in interpreting dissimilar polarisation effects provides further credence to the stream-based (fan-beam) geometry of pulsar emission. It also suggests that the microbeam width may not always be assumed negligible in comparison with the angular scale of emissivity gradients in the emission region.

Key words. pulsars: general – pulsars: individual: PSR J0437–4715 – pulsars: individual: PSR B1821–24A – radiation mechanisms: non-thermal.

1. Introduction

Pulsar polarisation escapes thorough understanding despite more than four decades of increasingly deep study, both observational and theoretical. The association of observed polarisation angle (PA, hereafter also denoted by ψ) with a projection of local magnetic field (Radhakrishnan & Cooke 1969) has strengthened the magnetic pole model of a radio pulsar beam. A mathematical formulation of this rotating vector model (RVM, Komesaroﬀ 1970) gives a chance to determine the global geometric parameters, such as the magnetic dipole inclination α and the viewing angle ζ , both measured with respect to the rotation axis Ω .

Because of the commonly encountered deviations of the observed PA from the simple RVM model, several extensions of the model have been made. Blaskiewicz et al. (1991) included the special relativistic effects on the PA curve (see also Dyks 2008), whereas Hibschman and Arons (2001) also included the modification of a local magnetic field by magnetospheric currents. Statistical studies of single-pulse PA distributions (McKinnon & Stinebring 1998, van Straten 2009) have shown the importance of various ways in which two polarisation modes can be combined in the presence of observational noise. Single-pulse analysis of polarisation (Edwards, Stappers & van Leeuwen 2003; Rankin & Ramachandran 2003) has shown a spatial (angular)

or temporal separation of orthogonal polarisation modes, interpreted either in terms of different refraction properties of these modes (Petrova & Lyubarski 2000; Lyubarsky 2008) or different locations of the modes in the radiation pattern of a specific emission mechanism (Dyks et al. 2010, hereafter DRD10). On the theoretical side, the convolution of a spatially extended emission with microphysical radiation beams has been numerically studied for non-coherent emission processes (Wang et al. 2012, Kumar & Gangadhara 2012) with the inclusion of possible propagation effects on the observed polarisation properties (Barnard & Arons 1986; Wang et al. 2010; Beskin & Philippov 2012). In these studies, the angular size of the microphysical radiation pattern was negligible in comparison to the angular gradients of emissivity in the emission region. Instead, in this paper we assume that these scales are comparable.

Via statistical modelling of single-pulse effects, Luo (2004) has shown that the microbeam effects are capable of generating perceivable non-RVM distortions when radio waves decouple from the local plasma close to the emission region. Melrose et al. (2006) have shown that statistical properties of single-pulse emission in both polarisation modes considerably influence the PA distributions observed at a fixed phase, hence they affect the average PA curve. By assuming appropriate populations of sin-

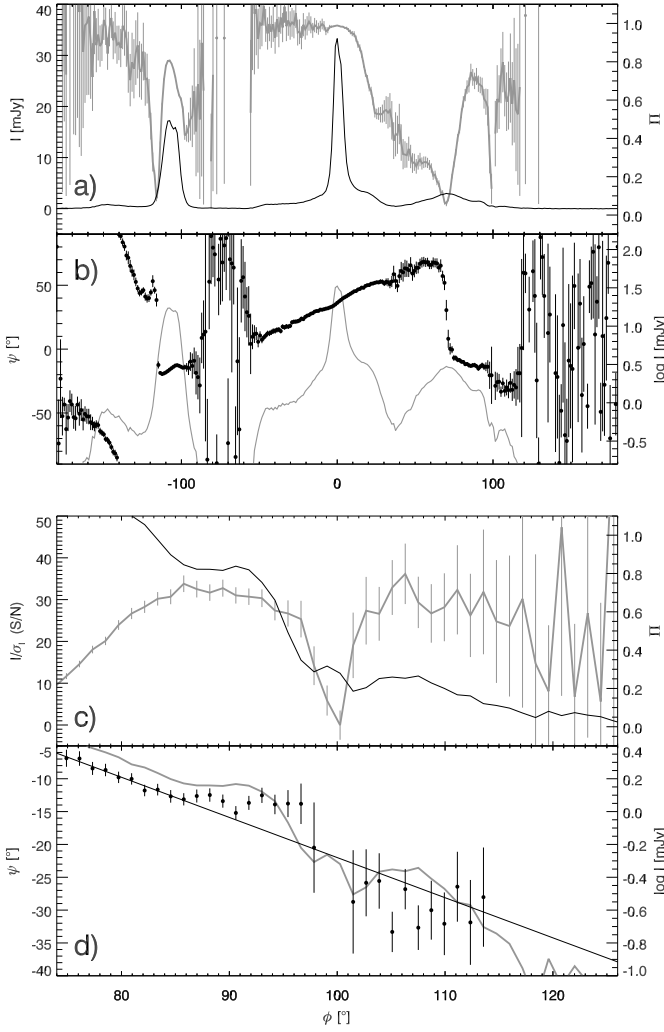


Fig. 1. Linear polarisation properties of PSR B1821–24A as observed with GBT in L band (BPDR). Grey curves refer to the vertical axes on the right-hand side. The bottom two panels zoom into the double notches at $\phi \approx 100^\circ$. **a)** Total flux I (black solid) and the linear polarisation fraction $\Pi = L/I$ (grey). **b)** The PA (black) and $\log I$ (grey). **c)** The total flux S/N (black solid) and the polarisation fraction (grey). **d)** The PA (black) and $\log I$ (grey). The straight line presents the PA variations anticipated in the absence of the notches. There is a drop in Π and a change in PA at the notches. The zero point of PA (whether observed or modelled) is arbitrary in all figures of this paper.

gle pulses, they were able to reproduce non-trivial distribution of data on the Poincare sphere.

In spite of these developments, it is usually impossible to explain why specific deviations of the average PA curve from the RVM model are observed. Notable exceptions are the orthogonal-mode jumps in PA by about 90° , which clearly originate from one mode being overtaken by its orthogonal counterpart (Cheng & Ruderman 1979, hereafter CR79; Tinbergen 2005). In this paper we attempt to understand less obvious distortions of PA, using a simple physical model of a polarised radiation beam, and convolving it with a macroscopic spatial distribution of emissivity. Our approach may be considered complementary to that of Melrose et al. (2006) who modelled the statistical effects of polarised single pulses at a fixed phase. We instead focus on how the microbeam topology relates the PA at

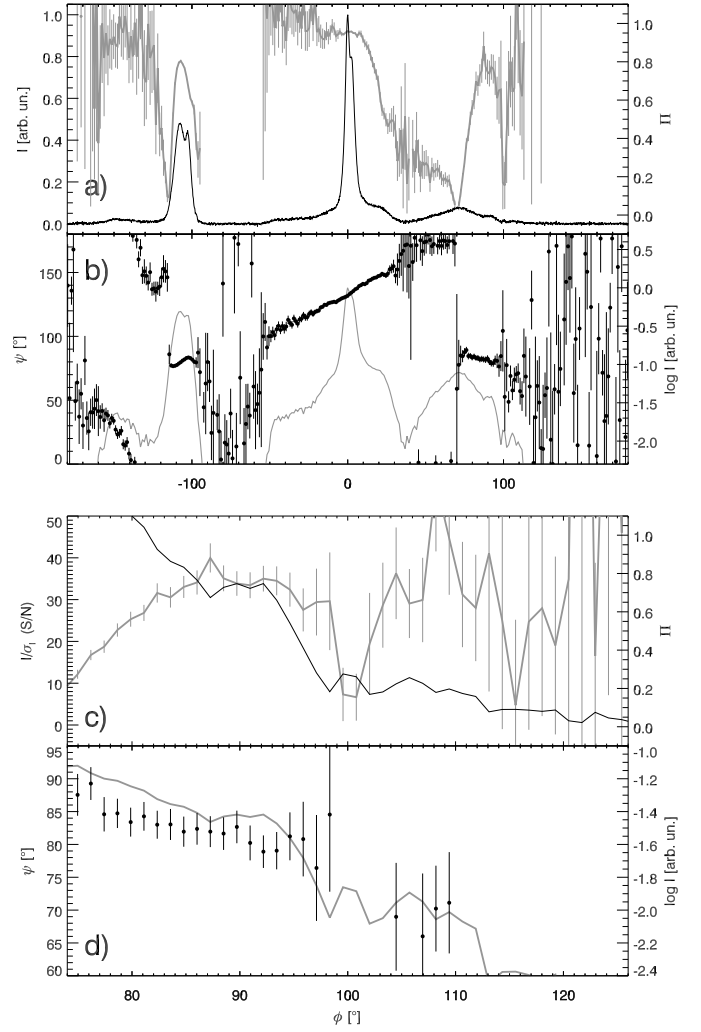


Fig. 2. Linear polarisation properties of PSR B1821–24A observed at 1.5 GHz with the Nançay telescope. The layout is the same as in Fig. 1. The total profile in a) has 2048 samples per period P , whereas resolution of the other data was decreased to 292 bins/ P by merging seven adjacent bins.

adjacent pulse longitudes while ignoring most of single-pulse effects. The non-RVM PA distortions may also be caused by multiple (Mitra & Li 2004) or radially extended (Dyks 2008) emission heights, return currents (Ramachandran & Kramer 2003), and scattering in the interstellar medium (Karastergiou 2009). None of these effects is included in the present study. Our model has been inspired by the high-quality observations of double notches reported for PSR B1821–24A in Bilous et al. (2015, hereafter BPDR; see Figs. 1 and 2 therein). However, the model is also applicable to the notches and the bifurcated emission component observed on the trailing side of the profile of PSR J0437–4715 (Navarro et al. 1997).

Section 2 describes available polarisation data for pulsars with double features in their average profiles. It is then followed by the description of model assumptions and the numerical method (Section 3). Section 4 presents the results of the model simulations, which are immediately compared to the observations.

2. Observed polarisation of profiles with double features

Bilous et al. (2015) reported high S/N L-band polarimetric observations of a 3.05-millisecond pulsar B1821–24A, which are summarised in our Fig. 1. The profile mostly exhibits a high linear polarisation fraction $\Pi = L/I$ except for two quasi-orthogonal polarisation jumps at $\phi \approx -117^\circ$ and 72° . A considerable drop in Π , however, also occurs at $\phi \approx 100^\circ$ where the double notches with a low, shallow central bump are found. Interestingly, even though Π decreases to nearly zero (grey line in Fig. 1c) the PA changes just a little bit, by approximately 15° (Fig. 1b and d). Although this change in PA has been described as a jump in BPDR, it may also be interpreted as a zigzag-shaped wiggle around a monotonically decreasing PA (marked with the straight line in Fig. 1d). This work provides a framework which supports this interpretation. In addition to the PA change at the phase of 100° , the profile of B1821–24A exhibits other interesting deflections from a smooth PA curve. There is a zigzag-like wiggle at the second-brightest component (P1, located at $\phi = -107^\circ$) and a one-directional PA deflection near the brightest component (P2, located at $\phi = 0^\circ$). They are associated with a larger Π and deviate from a smoothly interpolated PA curve less than observed at the double notches. Both P1 and P2 reveal a double structure, although they are not as well resolved and not as symmetric as the prominent double features observed in other pulsars (e.g. the bifurcated precursor of J1012+5307, DRD10). The slight PA distortions associated with these emission components will be addressed in Section 4.5.

2.1. Observations of B1821–24A with the Nançay Radio Telescope

The S/N of the profile within the notches observed by BPDR is ≈ 10 (black solid line in Fig. 1c), which is relatively low. This persuaded us to confirm the presence of the notches using independent observations. PSR B1821–24A is regularly observed with the 100 m equivalent Nançay Radio Telescope (NRT) as a part of its pulsar timing program. In order to obtain high S/N profile we used 82 observations taken between August 2011 and May 2015 approximately once every two weeks.

The data were recorded with the NUPPI backend (Liu et al. 2014) – a flexible digital signal processor designed for pulsar observations. First, Nyquist sampled spectra were acquired centred at 1484 MHz in 512 MHz bandwidth with 4 MHz resolution producing 128 frequency channels. The data were coherently dedispersed in real time using a dispersion measure value of $119.894 \text{ pc cm}^{-3}$ in order to correct for the dispersive delay caused by the interstellar medium (ISM). The data were then transformed from XY auto- and cross-correlations to full Stokes parameters, folded into final full-Stokes pulse profiles with resolution of 2048 samples per period and written out to disk in PSRFITS (Hotan et al. 2004) format. Each of the 82 observations was then inspected offline for the presence of radio-frequency interference (RFI) using standard pulsar processing tools (PAZ, PSRZAP) from the PSRCHIVE pulsar processing suite (Hotan et al. 2004) by zero-weighting the affected portions of the data.

Flux and polarisation calibration were also performed using the PSRCHIVE software package. A locally generated standard pulsed noise source was recorded to determine the flux scale. The equivalent noise source flux density was obtained by observation of the unpolarised quasar 3C48. Regular observations of linearly polarised pulsar B1929+10 were used to characterise the receiver system's intrinsic polarisation cross-coupling matrix

(van Straten 2004). The data was then corrected for the effects of rotation measure (RM) using the PSRCHIVE tool RMFIT. This resulted in an average profile with a total integration time of 49.2 hours ($\approx 5.8 \cdot 10^7$ periods).

The black solid line in panel a of Fig. 2 presents the average profile with 2048 samples per period. To increase the S/N, the rest of the observables in Fig. 2c are plotted after merging seven adjacent bins for a total of 292 samples per period, which is close to the resolution of the BPDR profile. Although the S/N of the Nançay profile is slightly lower, it does confirm the existence of the double ‘absorption’ feature at $\phi \approx 100^\circ$. As in BPDR, the two minima seem to be separated by an indistinct bump. Our data also confirm the change in PA, and the steep decrease in Π nearly to zero at the centre of the notches. In the Nançay profile P1 and P2 are both clearly double.

Polarised profiles of B1821–24A are also published by Dai et al. (2015), who present the Parkes data at 10, 20, and 50 cm. The change in PA at the phase of the notches is detectable there; however, the double form of the notches or of P1 and P2 is not resolved. The linear polarisation fraction Π considerably decreases within the notches (from 0.72 to 0.37, Fig. A16 therein), although not down to the near-zero value reported in BPDR. The difference may result from the smearing apparent in the Parkes profile.¹

Generally, all available data are consistent with the existence of double ‘absorption’ feature at $\phi \approx 100^\circ$, accompanied by the considerable drop in Π and a modest change in the PA value. Bilous et al. (2015) note that giant pulses in B1821–24A occur at the phase of the double notches, and a peak of a narrow component in an X-ray profile of this pulsar nearly coincides with the notches.

2.2. Linear polarisation of PSR J0437–4715

Another pulsar that will be discussed in terms of our model is PSR J0437–4715, a 5.25 ms pulsar with a long observation record at the Parkes telescope (e.g. Navarro et al. 1997; Osłowski et al. 2014; Dai et al. 2015). Its polarisation properties exhibit interesting similarities to and differences from the case of B1821–24A. Figure 3 summarises the best available linear polarisation data from Dai et al. (2015).² Double notches in J0437–4715 lag behind the peak of its brightest component by approximately 69° and have a pronounced central maximum, reaching a large fraction of the flux observed outside the notches. The linear polarisation fraction Π is decreasing at the minima of the notches by 20–30 per cent of the off-notch value (from 0.75 to 0.6 at the leading-side notch, and by more than a quarter at the trailing notch; see the grey line in Fig. 3c). At each minimum, the PA deflects toward the same direction by $\Delta\psi \approx 5^\circ$, which is a different behaviour from B1821–24A. Several other deflections of PA are observed across the profile, including the zigzags in the phase intervals marked with the rectangles in Fig. 3b: $\phi \in (-70^\circ, -48^\circ)$, $\phi \in (-40^\circ, -10^\circ)$, and $\phi \in (10^\circ, 32^\circ)$. These wiggles seem to coincide in phase with broad minima in total intensity, centred at $\phi \approx -60^\circ$, -25° , and 20° .

There are two more pulsars which exhibit both double notches and PA deflections: B1929+10 and B0950+08. In the

¹ The minimum Π measured by BPDR is eight times smaller than its statistical error, hence this data point is not plotted in panel a of Fig. 1, which only shows the points with $\Pi > \sigma_\Pi$, where σ_Π is the statistical error of Π .

² The data were obtained from the Parkes Observatory Pulsar Data Archive (Hobbs et al. 2011, dx.doi.org/10.4225/08/54F3990BDF3F1).

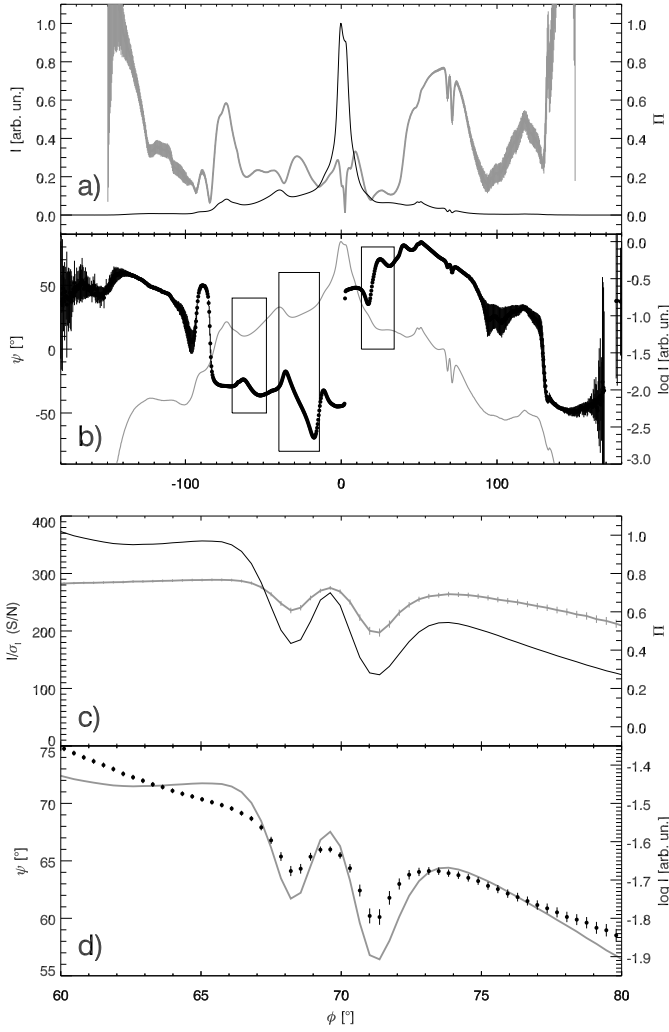


Fig. 3. Linear polarisation properties of PSR J0437–4715 observed at 1.4 GHz with the Parkes telescope (Dai et al. 2015). The layout is the same as in the previous figures. The rectangles in b) mark the zigzag-shaped PA distortions that are discussed in Section 4.3.

first, the notches are observed at a flux level hundreds of times lower than the peak of its main pulse. Well-calibrated polarisation data for this weak emission component are not available ($L > I$ in Rankin & Rathnasree 1997). In the case of B0950+08 the polarisation at 1.4 GHz was published in McLaughlin & Rankin (2004), however, for a profile with almost invisible notches, and with a small S/N in L .

3. A model for the polarisation angle deflections

The model assumes that the generic element of a radio emission region in a pulsar magnetosphere has the form of a plasma stream occupying a narrow magnetic flux tube (see Fig. 1 in Dyks & Rudak 2012, hereafter DR12). In a short time interval (quasi-instantaneously), the charges in the stream emit a narrow pattern of radiation beamed nearly along the velocity vector and pointed tangentially to the stream. The angular size of such a microbeam is small but significant, and it needs to be convolved with the spatial extent of the emission region (e.g. with the lateral profile of density or emissivity in the stream). When modelling the polarisation of notches we assume that the emitted mi-

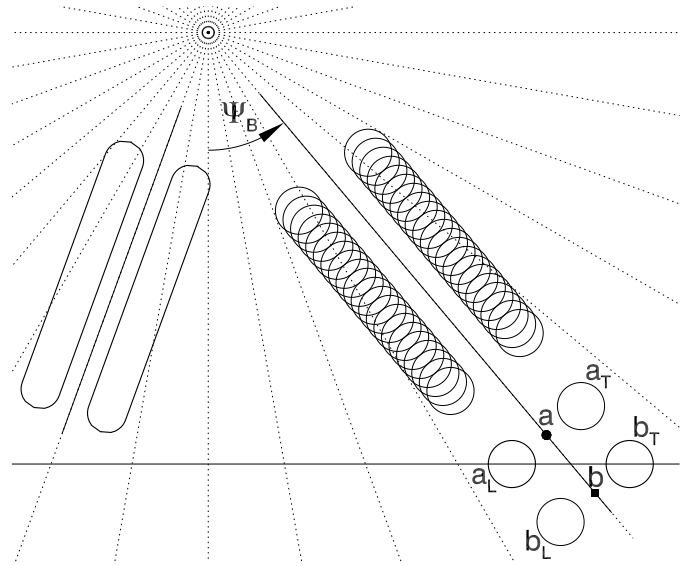


Fig. 4. Sky-projected view of the split-fan beams typical of the X-mode curvature radiation from narrow plasma streams. The continuous beam shown on the left can be decomposed into a sequence of lobe pairs, emitted quasi-instantaneously from different points along the stream (shown on the right-hand side), e.g. from the points ‘a’ and ‘b’ in the bottom right corner. The horizontal line marks the passage of the line of sight. The stream’s polarisation angle Ψ_B is detectable at two pulse longitudes (corresponding to the lobes a_L and b_T) on the leading and trailing side of the stream.

crobeam has the form of two lobes emitted at a small angle with respect to the plane of the magnetic field (see Fig. 1 in DR12, and Figs. 10 and 11 in DRD10). No radiation is emitted within the plane of the electron trajectory (which in this paper is assumed to coincide with a B -field line). Therefore, charges sweeping along a bent magnetic field, emit a split-fan beam shown on the left-hand side of Fig. 4.

Because the beam is double, each point of the stream (e.g. point ‘a’ in Fig. 4) creates two bright patches of emission on the sky (a_L and a_T). Therefore, a fairly localised piece of emission region, (e.g. the stream segment between ‘a’ and ‘b’ in Fig. 4) can be detected at two different phases in the profile. For the sightline passing along the horizontal path in Fig. 4, the a-b segment will be detected at the lobe a_L and b_T .

The process of curvature radiation (CR) in the extraordinary polarisation mode (hereafter the X mode or \perp -mode) provides an example of such a double-lobed beam. The CR beam emitted in vacuum can be mathematically decomposed into two parts: a filled-in pencil beam polarised in the plane of the B -field and the bifurcated beam polarised at the right angle to the plane of B (see Eq. 6.29 in Rybicki & Lightman 1979; Konopinski 1981, p. 305). In a strongly magnetised plasma, the emitted beam gets decomposed into a similar filled-in part polarised parallel to the B -field line plane (O mode) and a bifurcated X-mode part. In the limit of plasma in infinite magnetic field, only the X mode is emitted, again with the bifurcated beam pattern, and polarised at a right angle with respect to the B plane (Gil et al. 2004). To study the qualitative implications for the observed PA, it is sufficient to use the vacuum formula for the beam shape, which we do in Sect. 3.1 (Eq. 1).

In the quasi-instantaneous X-mode beam, however, the radiation is polarised in the $\mathbf{k} \times \mathbf{B}$ direction (see Fig. 1 in CR79 or

Fig. 16 in DRD10), where \mathbf{k} is the wave vector pointing towards the observer. The quasi-instantaneous polarisation direction then strongly depends on where exactly our line of sight is piercing the microbeam. A moving charge is passing this microbeam through our line of sight in a nanosecond timescale ($\Delta t \sim 1/\nu$, where ν is the observed frequency). During that time, a limited segment of the charge's trajectory of length $\Delta s \sim c\gamma^2\Delta t$ is exposed to the observer. For the charge's Lorentz factor of $\gamma \sim 10^2$, the detectable segment is few kilometers in length. The horizontal motion of the sightline through the lobe a_L in Fig. 4 is several orders of magnitude slower than the fast sweep of the lobe along the guiding magnetic field line. Therefore, if the emissivity does not change along that detectable part of electron trajectory, the observer is exposed to a time-symmetric signal of intensity and an antisymmetric signal of PA. These symmetries ensure that the net PA is orthogonal to the projected B -field for an arbitrary location of sightline in the fully swept-by beam (the split-fan beam).³

Accordingly, the lobe a_L , after fully passing through our line of sight, will contribute the PA fixed at the phase-independent value of $\psi_B = \Psi_B + 90^\circ$, where Ψ_B is the PA corresponding to the sky-projected direction of the magnetic field at point 'a'. Analogically, the trailing-side lobe b_T will be polarised at the same angle ψ_B , because the same magnetic azimuth corresponds to the emission point 'b'. If the emissivity and curvature of the B -field line do not change considerably between points 'a' and 'b', a symmetrical double-peaked emission component will be observed. It will be highly polarised and have a phase-independent PA.

The key assumptions of our model are then the following: 1) At least some parts of average profiles (especially those which exhibit bifurcated features) consist of elementary radiation patterns which have the double-peaked cross section such as shown by the dot-dashed line in Fig. 5a. This one-dimensional version of the microbeam pattern (denoted I_{mb}^\perp) needs to be convolved with the macroscopic distribution of emissivity η_\perp within the radio-emitting region; 2) It is assumed that both lobes of the microbeam are highly polarised at a fixed angle (of 90° for the X mode) with respect to the projected direction of the magnetic field line at the emission point corresponding to the observed lobes. A reference will be provided by the RVM PA value for the X mode (ψ_B) or the O mode (Ψ_B).

3.1. Numerical method

Double notches and bifurcated emission components are believed to be caused by a single void or peak in the spatial emissivity profile η_\perp . The double form results from the bifurcated nature of the microbeam which is convolved with this spatial emissivity (DRD10; DR12; cf. older models based on different concepts: Wright 2004; Dyks et al. 2007). Therefore, we start with a choice of the macroscopic emissivity η_\perp as a function of phase. In most cases we assume that η_\perp has a narrow Gaussian dip (or peak) carved in (or projecting from) a uniform emission component. An example of this η_\perp is presented by the thick solid line

³ This condition of uniform emissivity applies to each electron individually. However, the single-pulse emission, as determined by the longitudinal plasma density profile in the stream among others, may exhibit arbitrary variability. For this reason, the model is consistent with the observed randomness of subpulse shapes (cf. Sect. 3.2 in Luo 2004). However, it is not generally applicable for any pulse components, in particular those for which the single-charge emissivity is variable on the timescale of $\gamma^2\Delta t$ or those for which our sightline is just grazing the periferies of the full split-fan beam.

in Fig. 5a. This emissivity is convolved with the perfectly symmetric elementary emission pattern (dot-dashed line in Fig. 5a). We neglect a possible asymmetry of this micropattern, that may appear while the charges move between points 'a' and 'b' in Fig. 4. Such asymmetry (and a related distortion of PA) is generally expected when the radio emissivity varies with altitude and the sightline traverses through the split fan at an oblique angle (see Fig. 2 in DR12). Therefore, the dot-dashed line in Fig. 5a presents an effective pattern of the microbeam, mostly formed by emission from different points ('a' and 'b' in Fig. 4). For the effective microbeam shape we take that part of the vacuum CR beam which is polarised orthogonally to the plane of a B -field line

$$I_{mb}^\perp \propto \xi K_{1/3}^2(y) \sin^2(\phi - \phi'), \quad (1)$$

where

$$\xi = 1/\gamma^2 + (\phi - \phi')^2, \quad y = \frac{2\pi\nu\rho_{crv}}{3c} \xi^{3/2}, \quad (2)$$

K is the modified Bessel function, ϕ' is the phase of the microbeam centre, and γ is the Lorentz factor of the emitting particles (Rybicki & Lightman 1979). The magnification of the apparent microbeam through the non-orthogonal sightline cut at a possibly small α (section 2.2 in DR12) is ignored, i.e. the observed width of the microbeam Δ is set only by the values of ρ_{crv} and ν . The latter are selected to make the microbeam a few degrees wide in the observed profile. The Lorentz factor γ is fixed at a large (but otherwise arbitrary) value, because neither the scale nor shape of the microbeam depend on γ , whenever $\gamma \gg (\nu\rho_{crv}/c)^{1/3}$. To perform the convolution, a prescription for the B -field-based (RVM) PA curve is selected. Since we focus on narrow phase intervals, we approximate the PA with a linear function of phase (straight dotted line in Fig. 5b). For each pulse phase ϕ , the contributed flux of the microbeam (centred at an arbitrary phase ϕ') is scaled by $\eta_\perp(\phi')$ and it is assumed to be fully linearly polarised at the angle $\psi_B(\phi')$. Thus, most of the flux cumulated at ϕ originates from two nearby phases on both sides of ϕ . Since these phases contribute their own values of ψ_B , the intrinsic distribution of PA at a fixed ϕ has a double-peaked form (Fig. 5b), with no radiation corresponding to the central value of $\psi_B(\phi)$. However, the average value of the observed PA, (denoted by ψ_\perp since it refers to the X mode only), is equal to $\psi_B(\phi)$. When doing the convolution, we make the normal transitions between I , $L = (Q^2 + U^2)^{1/2}$, $\psi = 0.5 \arctan(U/Q)$ and the Stokes parameters I , $Q = L \cos(2\psi)$, $U = L \sin(2\psi)$. The circular polarisation and propagation effects are not studied in this work.

4. Results

In this section we present typical PA distortions implied by the model and discuss them in the light of observations described in Sect. 2. When we refer to data, model parameters are selected manually to obtain a qualitative agreement.

4.1. Origin of PA deflections at double notches

The convolution of the microbeam (dot-dashed line in Fig. 5a) with the spatial emissivity η_\perp (thick solid line) produces the double feature shown by the thin solid line in Fig. 5a. This means that a microbeam such as the one shown in the bottom right corner of Fig. 5b (dotted line) is not contributing its PA at the blank gap around point D in the greyscale distribution of PA. The averaging of PA at the phase marked with C then leads to the upward

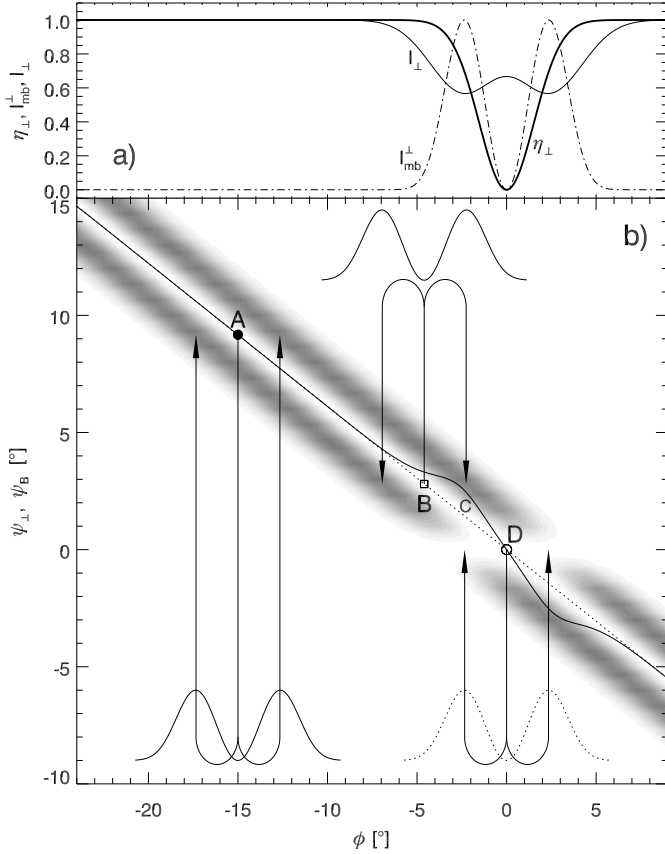


Fig. 5. Mechanism of the bidirectional (zigzag-shaped) PA distortion. **a)** Effective microbeam pattern I_{mb}^{\perp} (dot-dashed line), and the macroscopic X-mode emissivity η_{\perp} (thick solid) are convolved into the net intensity profile I_{\perp} (thin solid). **b)** PA as a function of phase. The slanted solid line marks ψ_{\perp} , i.e. the net value of the X-mode PA calculated as a fixed-phase average of the bifurcated grey band. The dotted line marks the RVM-based reference (ψ_B). The double-peaked microbeams, with arrows emerging from points A and B, show how the PA is distributed within the neighbouring pulse longitudes. The void assumed in η_{\perp} at D ($\phi = 0$) creates the horizontal break in the bifurcated PA band (grey). The resulting imbalance of the PA averaging produces the thick solid PA wiggle.

deflection of the net PA because the flux at C is dominated by emission from the phase B, with a larger PA. On the right-hand side of D, the same effect leads to a downward PA deflection of the same magnitude. The outcome is a zigzag-shaped wiggle of the net PA around the reference ψ_B .

Fig. 6 presents the calculation made for a Gaussian void in the emissivity: $\eta_{\perp} = 1 - \exp(-0.5\phi^2/\sigma_{\eta}^2)$, with $\sigma_{\eta} = 1.53^\circ$ (thick solid line in panel a), and for the microbeam of the apparent half size $\delta_{\text{mb}} = 2.34^\circ$ (dot-dashed line). The reference PA was assumed to change with phase at a rate similar to that observed in PSR B1821–24A: $\psi_B = -0.6\phi$ (dotted line in Fig. 6c; straight solid line in Fig. 1d). The net PA is shown in panel c by a thick solid line, which is made thinner in the central region of the notches where the observed PA is unavailable because of the insufficient S/N. There is a flattening of PA in the outer wings of the notches, which makes the impression of a discontinuous jump in PA similar to the one observed in B1821–24A. Panel b presents the intensity profile (thick solid line) and the linear polarisation fraction Π_{\perp} (top thin line). It is clear that the convo-

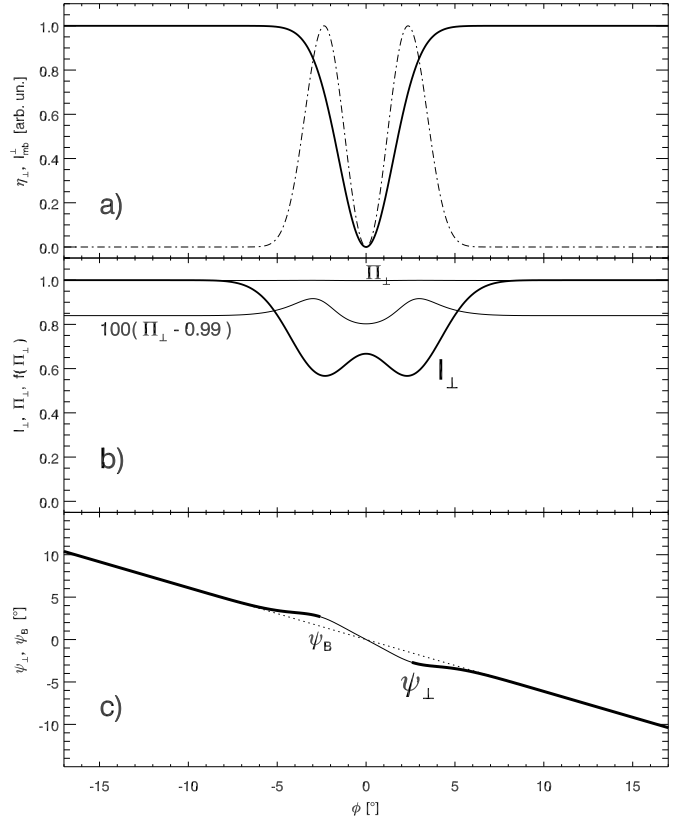


Fig. 6. Result of a calculation which produces the PA wiggle at a nearly merged double notch feature. **a)** Microbeam intensity I_{mb}^{\perp} (dot-dashed line) and the macroscopic emissivity with a Gaussian cavity at $\phi = 0$ (thick solid). **b)** Net polarisation fraction Π_{\perp} (top thin solid) and net X-mode intensity profile (thick solid). The Π_{\perp} is slightly smaller than 1, as shown by the bottom thin line presenting the quantity $100(\Pi_{\perp} - 0.99)$. **c)** Net X-mode PA (ψ_{\perp} , solid) overplotted on the reference ψ_B (dotted). The central part of ψ_{\perp} is thinner to reflect the lack of high-quality data points at the centre of notches in B1821–24A (see Figs. 1d and 2d). The result is for $\sigma_{\eta} = 1.53^\circ$, $\psi_B = -0.6\phi$, $\rho_{\text{crv}} = 5 \times 10^4$ cm, and $\nu = 1$ GHz.

lution of a single-mode (X-mode) radiation with similar values of PA (as constrained by the double-peaked PA distribution in Fig. 5b) does not produce perceivable depolarisation. A plot of $100(\Pi_{\perp} - 0.99)$ reveals that outside the notches Π_{\perp} drops by less than one per cent and is larger at the minima because the contribution of depolarising radiation (from a second lobe) is missing there. The modelled change in PA at the notches (by about 6°) is two times smaller than observed in B1821–24A.

The increase in Π_{\perp} and the small change in PA at the notches are inconsistent with the observations of B1821–24A; however, the result of Fig. 6 does not include the possible contribution of the other polarisation mode, i.e. the ordinary mode (O mode, or \parallel -mode), which is polarised parallel to the sky-projected B-field. In the following we use the term ‘net PA’ to describe the net (average) PA of a single polarisation mode (either X or O). For an average PA which contains both modes we use the term ‘total net PA’ (or just ‘total PA’).

4.2. Polarisation of notches in the presence of two modes

The effects of adding the O mode are illustrated in Fig. 7, calculated for the same parameters of the X mode as before. We have

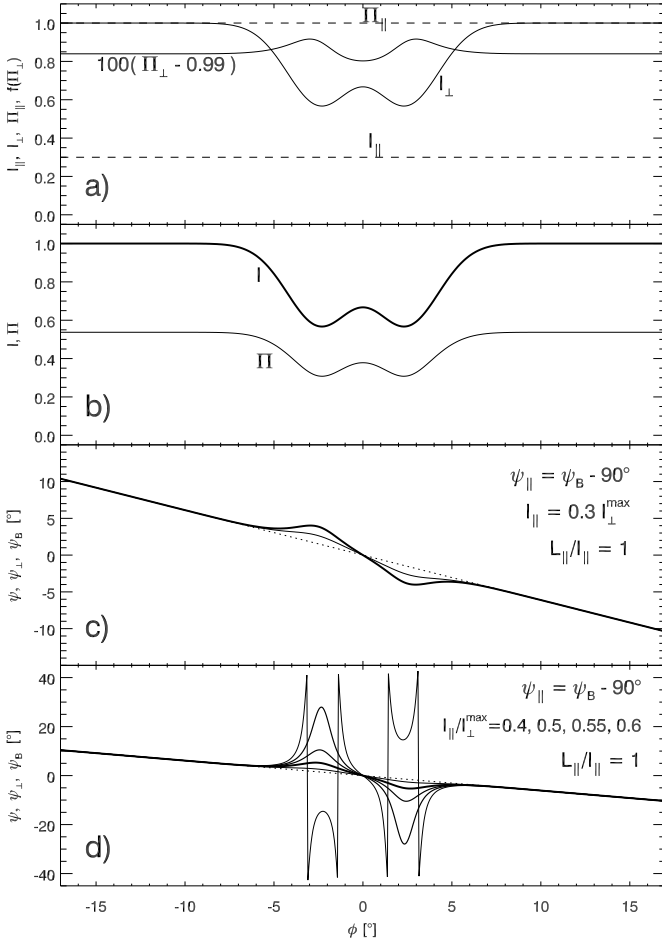


Fig. 7. Polarisation of double notches in the presence of two polarisation modes. **a)** Intensity and polarisation fraction for both modes (\perp -mode: solid line; \parallel -mode: dashed line). Π_{\perp} is indistinguishable from $\Pi_{\parallel} = 1$, hence we plot $100(\Pi_{\perp} - 0.99)$. **b)** Total intensity (thick solid line) and the total Π (thin line). **c)** Total PA ψ (thick solid line) overplotted on the net PA of the X mode (ψ_{\perp} , thin solid line), and the reference ψ_B of the RVM model (dotted line). The contribution of the O mode increases the off-RVM amplitude of the total PA. **d)** Same as in c, but for the increasing contribution of the O mode: $I_{\parallel}/I_{\perp}^{\max} = 0.4, 0.5, 0.55, \text{ and } 0.6$. The last case (thin line with spikes) undergoes the orthogonal-mode jumps. The unspecified parameters are the same as in Fig. 6.

added a fixed amount of the O mode ($I_{\parallel} = 0.3I_{\perp}^{\max}$) polarised strictly at a right angle with respect to the reference (RVM) PA of the X mode ($\psi_{\parallel} = \psi_B - 90^\circ$, i.e. the O mode is polarised along the projected B field). The linear polarisation properties of both modes are shown in panel a, with I_{\perp} referring to the net profile of the X mode (I_{\perp} results from the convolution of the curves shown in Fig. 6a). The total net profile (thick solid line in Fig. 7b) shows a drop in I down to 0.55 at the notches' minima. The total polarisation fraction Π (thin line in panel b) is now decreasing from 0.54 to 0.3, in qualitative agreement with the observations of B1821–24A. The wiggle of PA (panel c) extends over a larger interval because the O mode ‘attracts’ any non-orthogonal PA values to itself. The presence of the other polarisation mode then tends to magnify any slight deviations of the primary PA from strict orthogonality. Depending on the relative proportions of both modes, the amplitude of the wiggle can easily be arbitrarily increased. Fig. 7d, calculated for $I_{\parallel}/I_{\perp}^{\max} = 0.4$,

0.5, 0.55, and 0.6, presents how the PA deviation ($\Delta\psi = \psi - \psi_B$) grows with the increasing contribution of the \parallel -mode. For the selected parameters (i.e. for the assumed change in ψ_B across the microbeam width), $\Delta\psi$ exceeds 10° for I_{\parallel} approaching I_{\perp} with an accuracy of 10%. The largest distortion (for $I_{\parallel} = 0.6I_{\perp}^{\max}$, thin line with spikes) shows the jumps in PA by $\pm 90^\circ$ caused by the dominance of the O mode over the primary X mode at the minima of the notches.

The ease of obtaining such large distortions is an important phenomenon which has a crucial role in shaping the observed average PA curve: tiny distortions of PA from the reference ψ_B , become strongly magnified by the contribution of the other mode. The original (small) distortions in a single mode naturally result from the non-uniformity of the emission region (convolved with the properties of the microbeam). This makes the primary PA distribution at a given phase a little asymmetric with respect to the reference ψ_B . The incoherent contribution of the second polarisation mode can amplify these original PA deflections (characteristic of a single mode) to a very large magnitude, easily comparable to the 90° separation between the modes. When both polarisation modes have comparable flux, the net PA may be essentially arbitrary, which leads to the randomisation of the fixed-phase PA distributions described in McKinnon & Stinebring (1998) and Melrose et al. (2006).

At a fixed phase, each polarisation mode may then be expected to have the form of an intrinsic PA distribution with a finite width and with a specific shape, which is in general asymmetric with respect to ψ_B . Therefore, the PA ‘curve’ of pulsars should rather be understood as a PA stripe or band, as is frequently viewed in the greyscale plots presenting the PA distribution as a function of phase (e.g. Stinebring et al. 1984; Edwards & Stappers 2004; Hankins & Rankin 2010; Osłowski et al. 2014). The total net pulsar polarisation can be understood as the interaction of these two quasi-perpendicularly polarised bands of PA. Any skewness of such a PA stripe (i.e. of a single-mode PA histogram at a fixed phase) results in deflections which can be strongly enlarged by the second polarisation mode. However, if both polarisation modes are observed simultaneously, only the total distribution of PA may be perceivable at a fixed phase and the details of each mode PA distribution undetectable. As explained in Section 4.6, even if the pure X mode is detectable with negligible noise, the bifurcated PA distributions are unlikely to be observable. Our search for them in J0437–4715 was indeed unsuccessful.

The agreement of Fig. 7 with the polarisation data on the double notches in B1821–24A is qualitative only. For example, the modelled polarisation fraction Π does not decrease to such a low value as observed, and is actually slightly larger at the centre of the notches than at the minima. The amplitude of the modelled PA swing barely reaches 10° as compared to the observed value of 15° . There may be several reasons for these differences, and we discuss them in Sect. 5.

4.3. Interpreting the polarisation of PSR J0437–4715

The secondary (\parallel) polarisation mode is subject to different conditions of amplification and propagation (Melrose 2003; Wang, Wang & Han 2015; Beskin & Philippov 2012). It may undergo its own deflections from ψ_B , as determined by the skewness of O-mode PA distributions, resulting from the convolution of the O-mode emissivity with the O-mode microbeam. Since the mode is prone to additional propagation effects, e.g. a refraction, the PA of the O mode may possibly be even far from its RVM track. In this paper all these O-mode deflections are parametrised as a uni-

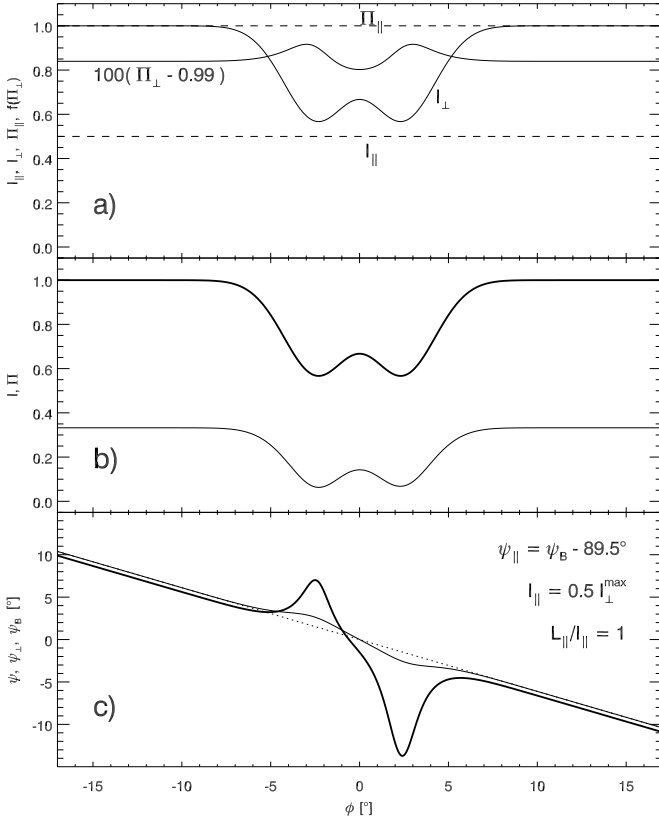


Fig. 8. Polarisation of double notches in the presence of a considerable amount of a quasi-orthogonal secondary polarisation mode ($\psi_{||} = \psi_B - 89.5^\circ$, $I_{||} = 0.5 I_{\perp}^{\max}$). The layout is the same as in panels a-c of Fig. 7. The PA wiggle in panel c acquired large amplitude and became asymmetric. Unspecified parameters are the same as before.

form shift of $\psi_{||}$ with respect to Ψ_B , where $\psi_{||}$ denotes the net PA of the parallel mode. We then assume $\psi_{||} = \Psi_B + \epsilon_{||} = \psi_B - 90^\circ + \epsilon_{||}$, with a small or moderate value of $\epsilon_{||}$. This simplification is done to make interpretation easier because in real data the total net PA results from an interplay of the X-mode deflections with the deflections of the O mode.

The summation of such quasi-orthogonal modes (Fig. 8c) slightly displaces the whole net PA curve towards $\psi_{||}$, increases the amplitude of the wiggle, and makes it asymmetric. The wiggle of Fig. 8c resembles those observed for J0437–4715 in the phase intervals: $(-70^\circ, -58^\circ)$, $(-40^\circ, -14^\circ)$, and $(13^\circ, 33^\circ)$ (indicated by rectangular boxes in Fig. 3b). As in our simulation, the observed wiggles seem to be associated with minima in intensity, revealed by the abrupt changes in the intensity gradient, e.g. at $\phi = -65^\circ, -10^\circ, 10^\circ$, and 15° . They may also be traced to double minima in Π (grey line in Fig. 3a). The wiggles may then be interpreted as the result of the ϕ -dependent skewness of the X-mode PA histogram, with the two-directional bias of PA induced by the broad absorption features. Since the observed width of these structures is several times larger than the scale of double notches, their origin is likely dominated by the effects of macroscopic emissivity.

In the case of J0437–4715, the PA at both minima of the double notches deflects in the same direction, which makes it different from B1821–24A. This behaviour readily appears in the model under some circumstances: when the linearly polarised X-mode flux drops considerably at the minima and the O mode is not too close to orthogonality with respect to the X mode (mod-

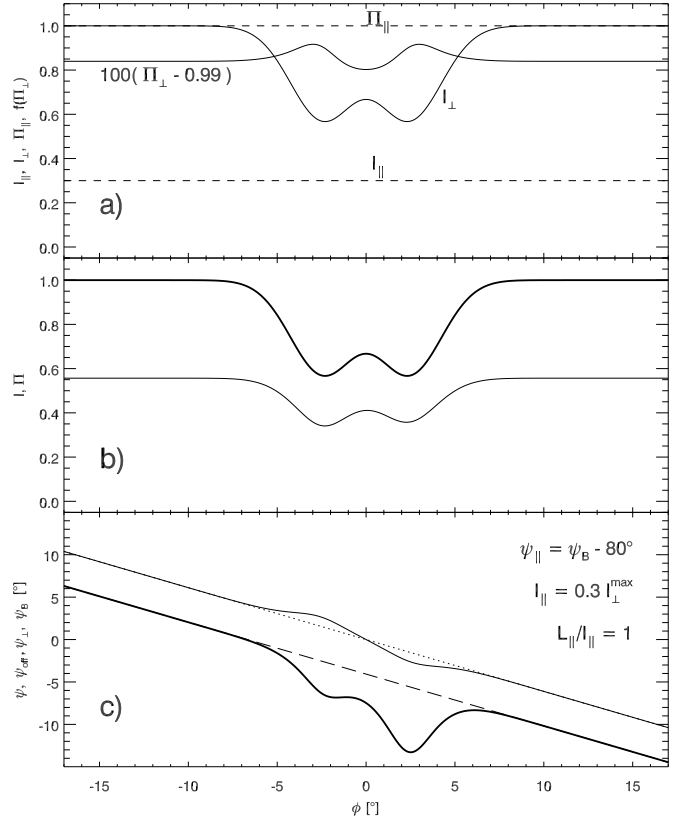


Fig. 9. Polarisation of double notches in the presence of a slightly non-orthogonal secondary polarisation mode ($\psi_{||} = \psi_B - 80^\circ$, $I_{||} = 0.3 I_{\perp}^{\max}$). The dashed line in c presents ψ_{off} , i.e. the interpolated off-notch trend of the total PA. The total PA at both minima is located below ψ_{off} (see the explanation in Fig. 10).

erate $\epsilon_{||}$). In Fig. 9c the O mode is 10° off orthogonality, so the overall PA curve is displaced down to the dashed line, which marks the interpolated off-notch trend ψ_{off} for the total PA. Even at the leading-side minimum ($\phi \approx -2^\circ$), where the net X-mode PA was above the RVM-based value ($\psi_{\perp} > \psi_B$), the contribution of the O mode drags the PA across ψ_B and we get $\psi < \psi_B$. Remarkably, however, the resulting value of the total PA at that phase is even smaller than ψ_{off} , so the PA at both minima stays below the dashed line.

The value of ψ at the centre of the notches does not undergo such a large shift and remains closer to ψ_{off} . The reason for which the PA at the leading-side minimum gets overdrawn to the other side of both ψ_{off} and ψ_B (as compared to its original location) is illustrated in Fig. 10. Because of the low polarised flux at the minima, the Stokes vectors representing $(L_{\perp}, \psi_{\perp})$ (marked with A and B in Fig. 10c) are shorter than the vector C which corresponds to the notches' centre. Therefore, the addition of the same $||$ -mode vector (representing the fixed amount of the parallel mode) is capable of inducing much larger rotation of PA towards $\psi_{||}$ at the minima. Without the drop in flux at the minima, this effect does not show up (Fig. 10b).

Fig. 11 presents a calculation performed to roughly reproduce the characteristics of the notches in J0437–4715. A rectangular void in η_{\perp} has been assumed to reproduce the large depth of notches with a high central maximum (the observed depth possibly approaches $\sim 50\%$, though the absolute zero flux level for J0437–4715 has not been determined rigorously). For $\psi_B = -0.9\phi$, $I_{||} = 0.3 I_{\perp}^{\max}$, and $\psi_{||} = \psi_B - 60^\circ$ the result roughly

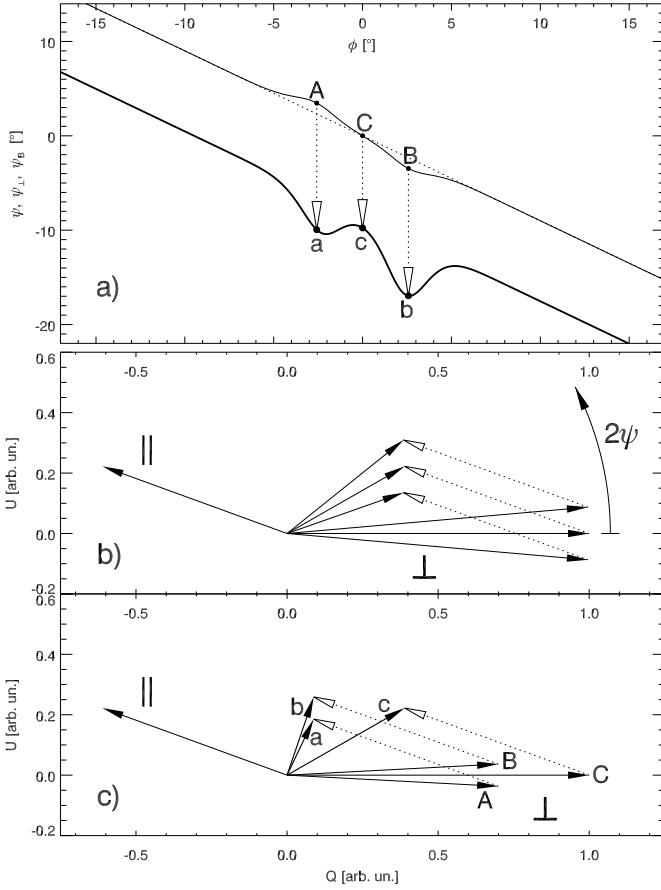


Fig. 10. Mechanism of transformation of the bidirectional PA distortion (the thin solid X-mode wiggle in panel a) into a one-directional W-shaped deflection of the total PA (thick solid). The Stokes vectors associated with the marked points are shown schematically in panel c. Those with small letters (a, b, c) are the sum of the corresponding X-mode vectors (A, B, C) with the quasi-orthogonal \parallel -mode vector shown on the left. The transition to the W-shaped PA is mainly caused by the drop in the X-mode flux at the minima of double notches (short vectors A and B). Panel b presents a similar sum for the case with no drop in polarised flux at A and B (all \perp -mode vectors have the same length).

reproduces the 20% drop in Π and the $\sim 5^\circ$ change in PA (the observed deflections are 4° at the leading-side minimum and 6° at the trailing minimum). The modelled deflection of PA reveals similar asymmetry. However, the drop in Π at the trailing minimum is a bit smaller than at the leading minimum, in contrast with observations (Fig. 3c). Possible reasons for these discrepancies are discussed in Sect. 5.

The observed PA exhibits an interesting behaviour at the bifurcated trailing component (BTC) in J0437–4715 (Fig. 12). On the right-hand side of the BTC, the PA appears to change linearly; however, it undergoes a step-like drop at the centre of the BTC (dots in panel b). Such a step-like change in PA is naturally expected in our ‘fixed-PA microbeam model’ if the emissivity η_\perp changes more steeply on the leading side of the BTC. Fig. 12 (c and d) presents a sample result obtained for η_\perp which rises quickly on the BTC’s left-hand side (following a Gaussian), but decreases linearly on the right (thick line in c). The step-like drop in PA occurs because the PA makes a transition from the single-lobe-dominated value on the left-hand side to the net

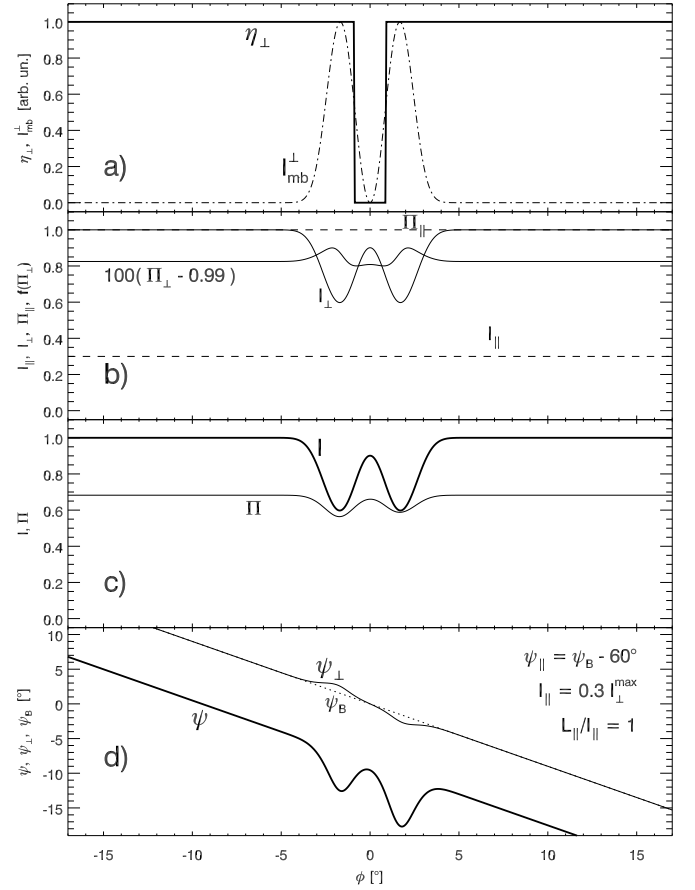


Fig. 11. Model results aimed at reproducing the observed properties of the double notches in J0437–4715 (see Fig. 3). A rectangular void in emissivity, of a half width equal to 0.9° (thick line in a), has been assumed to raise the central maximum of I at $\phi = 0$. The layout of panels b–d is analogous to panels a–c in Fig. 7. List of parameters: $\psi_B = -0.9\phi$, $\psi_\parallel = \psi_B - 60^\circ$, $I_\parallel = 0.3 I_\perp^{\max}$, $\rho_{\text{crv}} = 1.4 \times 10^5$ cm, $\nu = 1$ GHz.

value close to ψ_B on the right-hand side (see the thin solid curve for ψ_\perp in panel d). If a fixed fraction of the O mode is added ($I_\parallel = 0.3 I_\perp(\phi)$, $\Pi \approx 0.54$), then the total PA assumes the shape shown with the thick solid line in panel d. The model result does not reproduce the relative flux of the BTC’s peaks (see the thin solid line for I_\perp in panel c). However, the calculation does not take into account several factors that influence the ratio. These include 1) the likely asymmetry of the flux and PA in the effective microbeam, which appears for a non-orthogonal traverse of the sightline through a non-uniform split-fan beam (see Fig. 2 in DR12); 2) the profile of the O mode, the amount of which is increasing towards the left-hand side of the BTC, as suggested by the observed Π (grey line in a); and 3) the relative steepness of η_\perp on both sides of the BTC (a guess form of η_\perp was used in Fig. 12). Detailed modelling of this feature is deferred to a future study.

4.4. Non-bifurcated microbeam

In the case of the centripetal acceleration the ordinary mode is emitted into a single-peak microbeam of non-negligible width, such as that shown with the dot-dashed line in Fig. 13. We assume that the perceived PA is the same at any direction within the beam and equal to the projected direction of the B -field (Ψ_B).

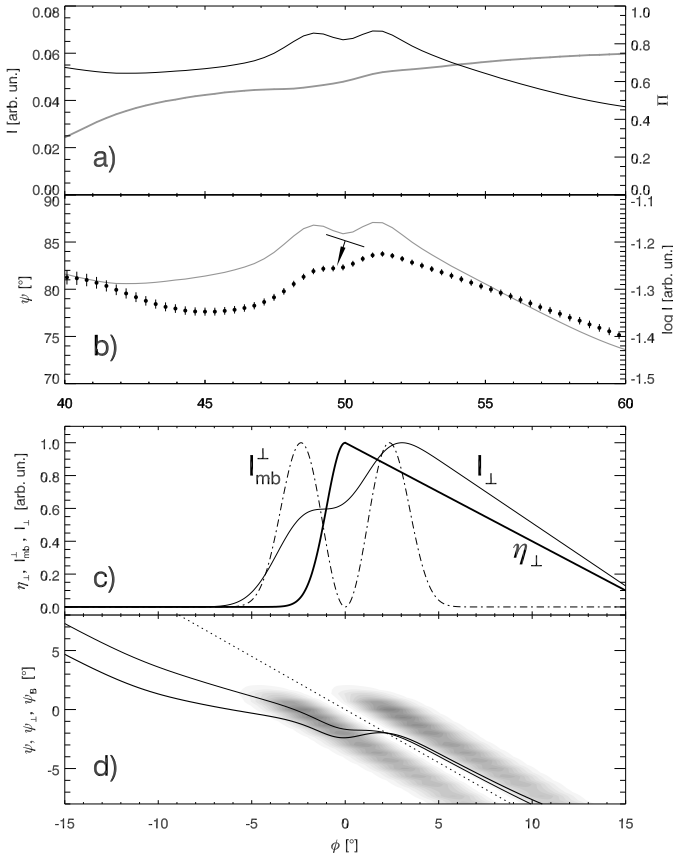


Fig. 12. Comparison of the observed (panels a and b) and modelled (c and d) properties of the bifurcated trailing component (BTC) in J0437–4715. The observed properties (I and Π in a; ψ and $\log I$ in b) present a zoomed part of Fig. 3. The arrow in b marks a step-like change in PA at the centre of the BTC (the PA is shown with dots). A similar step-like change in PA (solid lines in panel d) occurs for a one-sided emissivity profile (η_{\perp} , thick solid in c) which is decreasing gradually (linearly) on the right-hand side, but much more steeply on the left-hand side (a half-Gaussian with $\sigma_{\eta} = 1^{\circ}$). The thin solid line in d presents ψ_{\perp} , whereas the thick line presents ψ obtained for a fixed fractional contribution of the O mode: $I_{\parallel} = 0.3I_{\perp}(\phi)$. This is an exemplary result obtained for $\psi_B = -0.9\phi$, $\rho_{\text{crv}} = 5 \times 10^4$ cm.

In this subsection the void in the emissivity will be applied for the O mode only, η_{\parallel} refers to the macroscopic emissivity of the O mode, and $I_{\text{mb}}^{\parallel}$ represents the O-mode microbeam pattern. By analogy to the X mode (eq. 1), it is assumed that the O-mode microbeam can be approximated by that part of the vacuum CR beam which is polarised in the plane of the guiding B -field line, i.e. $I_{\text{mb}}^{\parallel} \propto \xi^2 K_{2/3}^2(y)$ (Rybicki & Lightman 1979).

If the other polarisation mode is absent, then a small-amplitude wiggle of PA also appears for the non-bifurcated O-mode beam. This occurs because the single-mode deflections depend on the asymmetry (or skewness) of the PA distributions at a fixed-phase. In the case of the single-peaked microbeam, the asymmetry is produced by the outer wings of its radiation pattern (Fig. 13). Because of the beam’s extension, a narrow dip in emissivity (thick solid line in panel a) results in the horizontal break in the grey PA distribution shown in panel b. The resulting fixed- ϕ histograms of PA, which are plotted every 1° below the grey PA band, are clearly skewed in opposite directions on either side of $\phi = 0^{\circ}$. The net PA then exhibits a wiggle similar

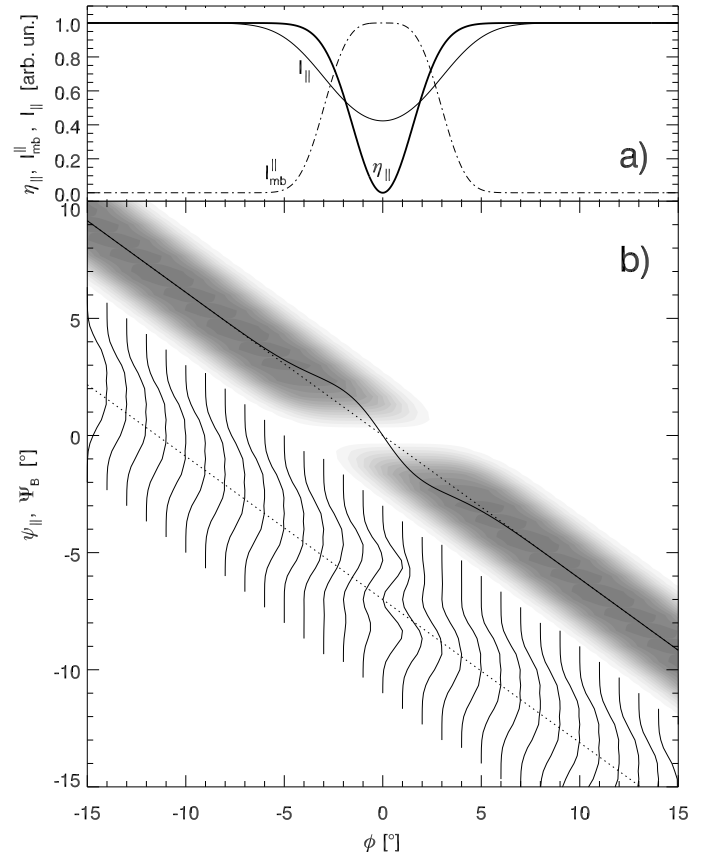


Fig. 13. Origin of the zigzag-shaped PA wiggle in the case of the filled-in microbeam of the O mode. The layout is similar to that of Fig. 5, except for the fixed-phase PA distributions which are plotted at 1° phase intervals in panel b. The minimum in η_{\parallel} produces the single-minimum dip in the net O-mode intensity (I_{\parallel} , thin solid line in a) as well as the blank gap in the non-bifurcated grey PA band (panel b). The PA wiggle is again produced by the imbalance of the PA averaging.

to the one for the bifurcated beam, albeit of a smaller amplitude. Close to $\phi = 0^{\circ}$, where the flux is low, the PA distribution becomes double (the fixed-phase PA histograms in Fig. 13b are normalised to the same peak value).

In the presence of both modes, however, the total PA has different properties than in the previously described case of the void convolved with the bifurcated microbeam. This occurs because the void in η_{\parallel} produces a single dip in I_{\parallel} , with the minimum value ($I_{\parallel} = I_{\parallel}^{\text{min}}$) at the centre ($\phi = \phi_{\text{min}} = 0$), whereas the maximum deflection of PA occurs in the wings of the feature (at $\phi_{\text{max}} \neq \phi_{\text{min}}$).⁴ Therefore, when the contribution of the other mode (X) is increasing, I_{\perp} first reaches I_{\parallel} at ϕ_{min} and produces the orthogonal PA jump there before it is able to considerably distort ψ at ϕ_{max} . If the modes are strictly orthogonal outside the notches ($\psi_{\perp} = \psi_B$ and $\psi_{\parallel} = \Psi_B$), a large-amplitude wiggle similar to those shown in Fig. 7d can only appear for finely tuned parameters: $L_{\perp} \approx L_{\parallel}(\phi_{\text{min}})$ (and $L_{\perp} < L_{\parallel}$) with accuracy of the order of 1%. Otherwise, the wiggle’s amplitude does not increase considerably or the PA jumps by 90° at ϕ_{min} . For modes

⁴ The subscript ‘min’ refers to the minimum flux of the primary polarisation mode (here I_{\parallel}), whereas ‘max’ to the maximum deflection of this primary mode PA from the reference PA (here $\Delta\psi_{\parallel} = \psi_{\parallel} - \Psi_B$). If the void is in η_{\parallel} , we have a single notch with $\phi_{\text{min}} \neq \phi_{\text{max}}$. For a narrow void in η_{\perp} , we have double notches with $\phi_{\text{min}} \approx \phi_{\text{max}}$.

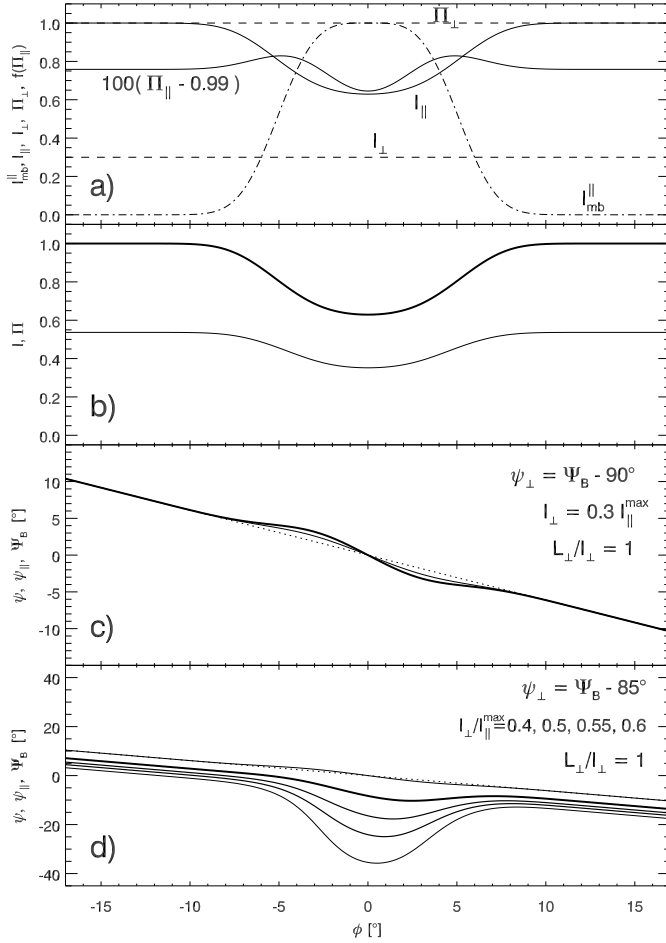


Fig. 14. Influence of the secondary polarisation mode (this time it is the X mode) on the polarisation of a single notch dominated by the primary O mode. A Gaussian void in emissivity $\eta_{||}$ of width $\sigma_{\eta} = 2.53^\circ$ is now applied only for the O-mode emission. The layout is analogous to that of Fig. 7, except in panel d the modes are not precisely orthogonal ($\psi_{\perp} = \psi_B - 85^\circ$). The contribution of the X mode does not much increase the amplitude of the PA wiggle in panel c (cf. Fig. 7c). The slight non-orthogonality of 5° (panel d) transforms the zigzag-shaped wiggle into a one-directional U-shaped distortion of PA (imagine a variant of Fig. 10c with the vector C shorter than A and B). List of parameters: $\psi_{||} = -0.6\phi$, $\rho_{\text{crv}} = 10^4$ cm, $\nu = 1$ GHz.

that are not exactly orthogonal ($\psi_{\perp} \neq \psi_B$), the bidirectional deflection of PA (i.e. the wiggle of Fig. 14c) quickly acquires a U-shaped form (Fig. 14d), i.e. it becomes a feature with a single minimum instead of either the zigzag shape or the W shape. This occurs because the total PA is mostly determined by the U-shaped drop in the net O-mode flux (see the curve for $I_{||}$ ($\approx L_{||}$) in panel a) and much less by the small zigzag deflection of the net PA (panel c). As shown in Fig. 10c, the total PA is mostly determined by the amount of the linearly polarised flux of the primary mode, rather than its PA. This flux ($L_{||}$) is minimal at the centre of the U-shaped feature, hence the largest deflection of the total PA occurs there (Fig. 14d). Thus, the total PA also follows a U-shaped curve, just like the $I_{||}$ (or $L_{||}$) does.

We then conclude that the lack of emission at the centre of the microbeam facilitates the appearance of the wiggle-shaped deflections of PA in the average profiles. This is consistent with the fact that the profiles of PSR J0437–4715 and B1821–24A

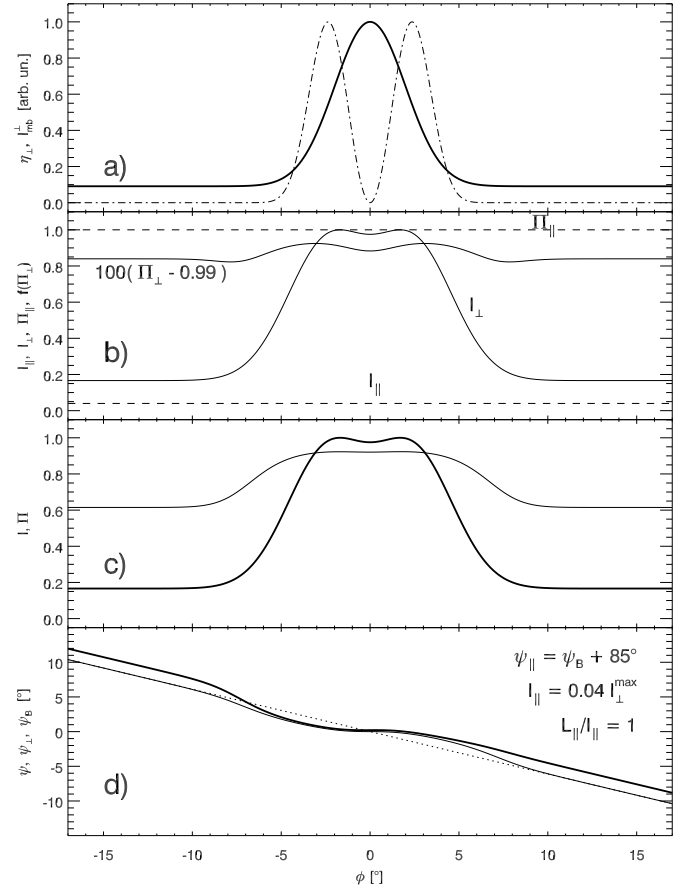


Fig. 15. Modelled polarisation of a bright narrow component projecting from an isotropic background emission. The PA curve exhibits a flattening under the component (panel d), caused by the fixed PA attributed to the microbeam. A small uniform contribution of the O mode ($I_{||} = 0.04 I_{\perp}^{\text{max}}$) produces the off-centred, one-directional distortion of PA (thick line in d). Used parameters: $\psi_{||} = \psi_B + 85^\circ$, $\rho_{\text{crv}} = 5 \times 10^4$ cm.

contain both the wiggle-shaped PA deflections and the bifurcated features (the notches and the bifurcated emission components).

4.5. PA deflections at profile emission components

In the case of PSR B1821–24A, some small distortions of PA appear under its two brightest components (P1 and P2), both of which are double. The wiggle of PA at the second brightest peak (P1 at $\phi = -105^\circ$ in Fig. 1) looks deceptively similar to the modelled distortion described for the absorption features (Figs. 6c, and 7c,d). On the other hand, the brightest peak in the profile of B1821–24A (P2 at $\phi = 0$ in Fig. 1), has the PA which deflects in one direction only (no zigzag) and the deflection is not phase-aligned with the peak; instead, it is located on its leading side.

As shown in Fig. 15, the fixed-PA microbeam model can easily produce off-centred one-directional PA distortions, albeit not of the type observed for the peaks of B1821–24A. Fig. 15 has been calculated for a slightly wider maximum in the X-mode emissivity, $\eta_{\perp} = 0.1 + 0.9 \exp(-0.5(\phi/2^\circ)^2)$, to reproduce the nearly unresolved main component of B1821–24A (P2). When a small amount (only $0.04 I_{\perp}^{\text{max}}$) of a quasi-perpendicular O mode is added ($\psi_{||} = \psi_B + 85^\circ$), the linear polarisation fraction stays very high within the component (panel c) and the total PA makes a

single deflection on its leading wing (thick line in d). The zigzag disappears because the convolution of the two modes aligns the off-notch trend of the total PA with the net X-mode PA in the trailing half of the component.

This result is somewhat similar to the observed one; however, unlike in the observation, the PA in Fig. 15 is decreasing with increasing pulse phase ϕ , i.e. the PA gradient $S = d\psi_B/d\phi$ is negative. Had we changed the sign of S to the observed (positive) value, the one-directional deflection would move to the trailing side of the peak, in conflict with the observation. Had we additionally changed the sign of the modal non-orthogonality (taking $\psi_{\parallel} = \psi_B - 85^\circ$), the total PA deflection would move to the leading side, but it would be protruding upward, again inconsistent with data. The reason is that the addition of a bright X-mode component to a low-level X-mode background always results in a flattening of the net PA gradient under the added component (thin solid line in Fig. 15d); whenever the microbeam width is larger than (or comparable to) the width of the peak in η_{\perp} , the added component contributes the fixed PA value, so a brightening in a profile should always be associated with the flattening of the PA curve. In contrast with this implication, the PSR B1821–24A (though not J0437–4715) exhibits increased $|S|$ under the bright emission components. A possible reason for this discrepancy may involve unrecognised single-pulse effects (cf. Melrose et al. 2006).

An observational detail that may be of great importance is that a single orthogonal-mode jump (at $\phi \approx 70^\circ$ in Figs. 1b and 2b) separates the P2 from the double notches in B1821–24A. Therefore, if the notches are interpreted as the signature of the bifurcated X-mode beam, the highly-polarised P2 (and also P1, with its PA being an extrapolation of the linear trend observed near P2) should be dominated by the O-mode emission in the form of the filled-in (non-bifurcated) beam. The bifurcations of the P1 and P2 should then probably be interpreted in terms of macroscopic properties of the emitter or in terms of propagation effects. A possible origin of such macroscopic bifurcations has been suggested in Dyks & Rudak (2015, see figure 12 therein).

Our model of polarisation (based on a wide microbeam) implies that any changes in flux in the profile must be unavoidably accompanied by small deviations of PA from the RVM. When the profile emission components extend for wide intervals of phase, and when the flux changes slowly, then the PA distortions are not visible as clear local features; however, the net PA is not likely to precisely follow the RVM-based value. This is shown in Fig. 16 where the X-mode η_{\perp} has the form of a wide triangle (thick solid in panel a). The gradual distortion of the net PA (flattening near the flux maximum) is visible in panel b.

4.6. Double-peaked PA distributions

The presented model is supported by the existence of the bifurcated features in the profiles of B1821–24A and J0437–4715. Superficially, however, one might expect a stronger support to come from a direct observation of the double-peaked PA distributions, such as shown in grey in Fig. 5b. The peaks of the pure X-mode PA distributions are separated by $\Delta|d\psi_B/d\phi|$, where Δ is the observed scale of double features. In most cases discussed before $|d\psi_B/d\phi| \sim 1$, thus the separation is of the order of a few degrees. We have searched for the PA bifurcations in J0437–4715 using the polarisation calibrated single-pulse data described in detail in Osłowski et al. (2014). The search was unsuccessful, even within this part of the profile which contains bifurcated features.

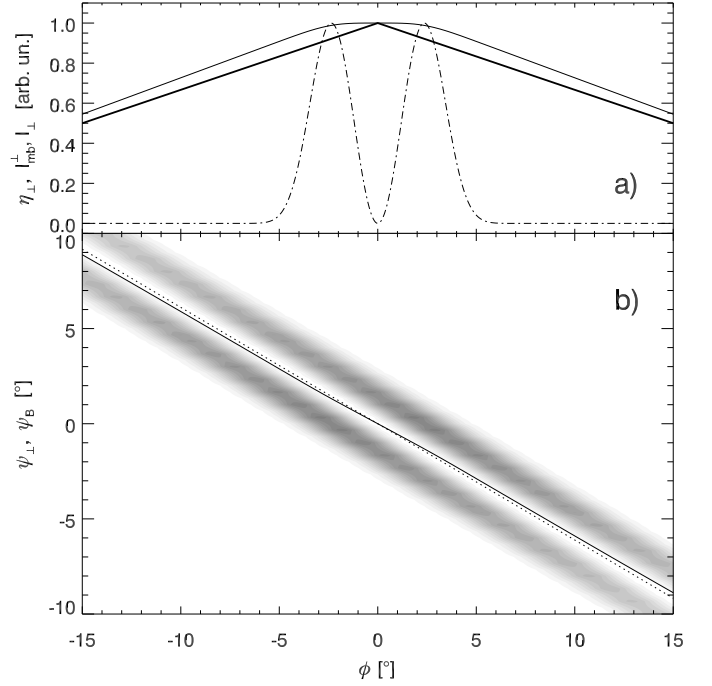


Fig. 16. Polarisation of a very wide emission structure with the triangular emissivity pattern shown in panel a (thick solid line). The net PA (solid line in panel b) nearly follows ψ_B , but not exactly.

This can be understood, however, and does not pose a problem for our model because the flux detected at any moment is a convolution of several intrinsic signals (not to mention the instrumental noise) which can strongly affect the observed two-dimensional (ϕ, ψ) distributions. Specifically, the flux in each peak of the double PA distribution (as observed at a fixed phase) corresponds to emission from two different (but nearby) phases, and two different (but closely located) emission points in the magnetosphere. For example, at the phase C in Fig. 5, one of the PA peaks originates from phase B, and another one from phase D. If the two emitting points permanently contribute both these PA peaks, only their average (close to ψ_B) will be detectable at any moment in single-pulse observations. Therefore, for the PA bifurcation to be visible even in the pure X mode, non-simultaneous contributions of flux from both phases should occur. During one star rotation, the flux at the considered phase would have to be strongly dominated by emission from one phase (e.g. B), during another rotation by the other phase (D). The bifurcation will be lost if the contributions are comparable and simultaneous. Since we discuss two nearby pulse phases and a laterally extended emission region, such temporal separation of emission seems unlikely, which explains why the PA bifurcations are not observed.

Thus, to see the bifurcation, the flux which contributes to one PA peak has to be received in different pulses (or at least in different samples) than the flux which contributes to the other PA peak. The PA values in both peaks may therefore be affected by the instrumental noise of different sign or strength. This additionally increases the difficulty of detection of the PA bifurcation, even when the conditions of the previous paragraph are fulfilled.

The detection may even be made more difficult by the simultaneous emission in both polarisation modes. In this case we observe the instantaneous total PA determined by the degree

of their non-orthogonality (and by the relative amounts of both modes).

We then conclude that the clear bifurcation of the X-mode PA, such as illustrated in Fig. 5b, is not likely to be detected unless several ‘purifying’ conditions are met. The main condition requires that the emission in each PA peak occurs in the above-described successive way, belonging either to the first or to the second PA peak. This is further complicated by the real-time instrumental noise, and the possible contribution of the O mode. Our model is then consistent with the ubiquitous lack of the PA bifurcations in pulsar data.

4.7. Multiple PA bands in pulsars

The issue of simultaneous emission of both polarisation modes is related to the possibility of observation of several non-orthogonal PA stripes on the (ϕ, ψ) plane. This phenomenon is reported, for example, for B1237+25 observed at 327 MHz at the Arecibo Observatory (Smith et al. 2013). A distinct PA stripe, which looks like a wiggle which is not parallel to the PA stripe of the primary mode, is observed under the central component in the profile of this object. If the primary mode is assumed to follow the RVM, the distinct additional wiggle may be interpreted as the PA stripe corresponding to the simultaneous emission of both modes. The primary PA stripe would then represent the undisturbed PA of the primary mode emitted mostly alone.

In the simplest case there are three distinct situations in which only the primary or secondary mode is emitted, or both modes are emitted simultaneously. Then at least three PA stripes can be produced on the (ϕ, ψ) plane, one corresponding to the primary mode, another to the secondary mode (if it happens to be emitted alone), and a third stripe for the simultaneous emission of both modes. The location of the last (non-RVM) stripe is determined by the intrinsic degree of non-orthogonality and the relative flux in both modes. As shown in Melrose et al. (2006), for a well-defined (sharp) extra PA stripe, the radiation emitted simultaneously must be characterised by a preferred (frequently occurring) combination of these parameters. Otherwise the PA becomes randomised (McKinnon and Stinebring 1998). Examples of such randomisation can sometimes be found in single-pulse PA data; see e.g. the profile of B1919+21 in Hankins & Rankin (2010) and . Thorough analysis of mode mixing effects is presented in van Straten & Tiburzi (in preparation).

5. Discussion

To account for observed PA distortions, a CR-based model can be set up which assumes emission into a bifurcated beam of non-negligible angular extent and polarised at a fixed angle with respect to the local B -field. This elementary beam (a microbeam) is convolved with an emissivity profile which represents the lateral extent of the emission region, and it is supplemented with a contribution of the secondary polarisation mode.

A model of such a type is capable of qualitatively reproducing the polarisation behaviour of several dissimilar features in the profiles of B1821–24A and J0437–4715. This provides additional support for the stream-shaped geometry of the pulsar emission region, and for the fan-shaped geometry of the pulsar beams (Michel 1987; DRD10; DR12; Wang et al. 2014; Dyks & Rudak 2015). It also shows that CR is a useful mechanism for interpreting the pulsar radio emission.

However, the model cannot reproduce the steepening of PA under emission components, nor the large drop in the polarisation degree at the centre of notches in B1821–24. The notches

may be created by a single non-emitting plasma stream embedded in a laterally extended emission region, or as a dense obscuring stream, located above the emission region (see fig. 12 in DRD10). If the bifurcation of the notches originates from the extraordinary-mode nature of the microbeam, then the non-emissive interpretation is favoured because the X-mode radiation does not interact with the plasma in the superstrong B -field; hence, it should not be absorbed or obscured. It is possible that the ‘dark’ stream is responsible for the giant pulses observed near the centre of the notches (Figs. 1 and 2 in BPDR). The stream may either be directly generating the giant pulse emission, or it may be reprocessing the background radiation of the surrounding emitter, e.g. via scattering of the radio photons. In either case the new type of radiation may have different polarisation properties from the surrounding background which could produce the extra depolarisation. It is important to note that such a contribution of extra emission at the centre of the double notches can mislead our modelling efforts since the height of the central maximum of double notches is the main factor which determines the width of the void in emissivity η_{\perp} .

The model predicts that the intrinsic bifurcation of the PA distribution at a fixed phase is unlikely to be detectable, unless special conditions are satisfied. These include not only the nearly pure X-mode emission (mostly free from the noise and the O mode), but also a sequential (non-simultaneous) detection of flux from two nearby pulse longitudes (those which contribute each PA peak at a considered pulse phase). The proposed model is therefore consistent with the lack of the PA bifurcations in the pulsar data.

Generally, the model illustrates the key importance of the circum-RVM distribution of PA for the shape of the average PA curve. Since the spread of PA at a fixed phase is intrinsic, it is worth thinking in terms of a PA band or stripe instead of a PA curve. These fixed-phase PA distributions are unlikely to be symmetrical around the RVM-based value, and any small deviations of one mode are amplified by the existence of the other polarisation mode. This can lead to large PA deflections in the averaged profiles, and to the PA randomisation in single pulses.

This work suggests that in several pulsars the angular scale of the microbeam is not negligible in comparison to the angular gradients of emissivity in the emission region. Many observed distortions from the RVM may result from the microscopic PA becoming recognizable despite the convolution with the spatial extent of the emitter.

The data reproduction achieved through the by-eye fitting described in Sect. 4 is qualitative only, and the main reason for this are the guessed and simple forms of η_{\perp} and η_{\parallel} . Instead, the observed polarised intensity profiles likely do not correspond to any simple analytical functions. For example, the notches in J0437–4715 seem to coincide with a broad emission bump superposed on a monotonically declining flux, whereas the BTC consists of η_{\perp} and η_{\parallel} , which cannot be described by a simple exponential or linear function. A possible solution to this problem would be to split the observed average profile into two fully polarised orthogonal modes, then deconvolve the microbeam from the mode-separated profiles to learn the approximate form of η_{\perp} and η_{\parallel} . Another development that may be needed is a three-dimensional code capable of simulating an oblique traverse through the fan beams (hence including the apparent asymmetry of the microbeam). Moreover, the single-pulse population effects (Melrose et al. 2006) have already been shown to crucially affect the apparent polarisation. They seem to be the most important ingredient that may need to be included in the modelling to achieve close agreement with the data. Thus, the ques-

tion of whether complicated average PA curves (such as that of J0437–4715) can be disentangled into their pure RVM form, remains open.

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